



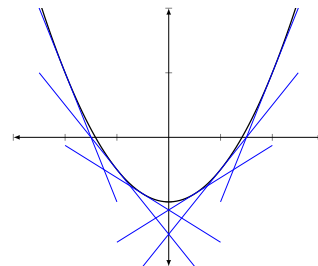
CALCULUS

DERIVATIVE RULES

DEFINITION OF THE DERIVATIVE

The **derivative** of $f(x)$ with respect to x is the function $f'(x)$ and is defined as

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} \quad \text{or} \quad f'(x) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$



Let c , b , and n be constants and f , g , functions of x .

$\frac{d}{dx}(c) = 0$	$\frac{d}{dx}(x) = 1$
$\frac{d}{dx}(c \cdot f) = c \cdot f'$	$\frac{d}{dx}(ax^n) = n \cdot ax^{n-1}$ (Power Rule)
$\frac{d}{dx}(f \pm g) = f' \pm g'$	$\frac{d}{dx}(c^x) = c^x \cdot \ln(c)$
$\frac{d}{dx}(f \cdot g) = f \cdot g' + g \cdot f'$ (Product Rule)	$\frac{d}{dx}\left(\frac{f}{g}\right) = \frac{g \cdot f' - f \cdot g'}{g^2}$ (Quotient Rule)
$\frac{d}{dx}(\ln(f)) = \frac{1}{f} \cdot f'$ for $f \neq 0$	$\frac{d}{dx}(\log_c(f)) = \frac{1}{f \cdot \ln(c)} \cdot f'$ for $f \neq 0$
$\frac{d}{dx}(e^f) = e^f \cdot f'$	$\frac{d}{dx}(f(g)) = f'(g) \cdot g'$ (Chain Rule)

TRIGONOMETRIC DERIVATIVES

$\frac{d}{dx}(\sin(x)) = \cos(x) \cdot x'$	$\frac{d}{dx}(\cos(x)) = -\sin(x) \cdot x'$
$\frac{d}{dx}(\tan(x)) = \sec^2(x) \cdot x'$	$\frac{d}{dx}(\csc(x)) = -\csc(x) \cot(x) \cdot x'$
$\frac{d}{dx}(\sec(x)) = \sec(x) \tan(x) \cdot x'$	$\frac{d}{dx}(\cot(x)) = -\csc^2(x) \cdot x'$
$\frac{d}{dx}(\sin^{-1}(x)) = \frac{1}{\sqrt{1-x^2}} \cdot x'$	$\frac{d}{dx}(\cos^{-1}(x)) = -\frac{1}{\sqrt{1-x^2}} \cdot x'$
$\frac{d}{dx}(\tan^{-1}(x)) = \frac{1}{1+x^2} \cdot x'$	<i>Note</i> : Here x' was shown to demonstrate the chain rule. In these examples, $x' = 1$, as it is the derivative of x .





CALCULUS

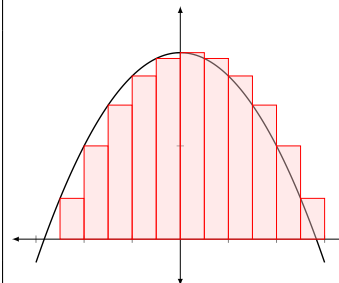
INTEGRAL RULES

DEFINITION OF THE DEFINITE INTEGRAL

If f is integrable on $[a,b]$, then the **integral** of $f(x)$ with respect to x is the function $F(x)$ and is defined as

$$F(x) = \int_a^b f(x) \cdot dx = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i) \Delta x$$

where $\Delta x = \frac{b-a}{n}$ and $x_i = a + i\Delta x$.



PERTINENT SUMS

$$\sum_{i=1}^n i = \frac{n(n+1)}{2}$$

$$\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$$

$$\sum_{i=1}^n i^3 = \left[\frac{n(n+1)}{2} \right]^2$$

FUNDAMENTAL THEOREM OF CALCULUS

If $f(x)$ is continuous on $[a,b]$, then the **integral** of $f(x)$ with respect to x from a to b is

$$\int_a^b f(x) \cdot dx = F(b) - F(a)$$

where $F(x)$ is an antiderivative of $f(x)$.

Let c , b , and n be constants and f, g , functions of x .

$\int c \cdot f(x) \cdot dx = c \int f(x) \cdot dx$	$\int [f(x) \pm g(x)] \cdot dx = \int f(x) \cdot dx \pm \int g(x) \cdot dx$
$\int dx = x + C$	$\int x^n \cdot dx = \frac{x^{n+1}}{n+1} + C$, for $n \neq -1$
$\int \frac{dx}{x} = \ln x + C$	$\int e^x \cdot dx = e^x + C$
$\int_a^a f(x) \cdot dx = 0$	$\int_a^b f(x) \cdot dx = - \int_b^a f(x) \cdot dx$
$\int \frac{1}{\sqrt{1-x^2}} \cdot dx = \arcsin(x) + C$	$\int -\frac{1}{\sqrt{1-x^2}} \cdot dx = \arccos(x) + C$

