



TRIGONOMETRY

LAWS AND IDENTITIES

QUOTIENT IDENTITIES

$$\tan(x) = \frac{\sin(x)}{\cos(x)}$$

$$\cot(x) = \frac{\cos(x)}{\sin(x)}$$

RECIPROCAL IDENTITIES

$$\csc(x) = \frac{1}{\sin(x)} \quad \sin(x) = \frac{1}{\csc(x)}$$

$$\sec(x) = \frac{1}{\cos(x)} \quad \cos(x) = \frac{1}{\sec(x)}$$

$$\cot(x) = \frac{1}{\tan(x)} \quad \tan(x) = \frac{1}{\cot(x)}$$

EVEN/ODD IDENTITIES

$$\sin(-x) = -\sin(x) \quad \csc(-x) = -\csc(x)$$

$$\cos(-x) = \cos(x) \quad \sec(-x) = \sec(x)$$

$$\tan(-x) = -\tan(x) \quad \cot(-x) = -\cot(x)$$

PYTHAGOREAN IDENTITIES

$$\cos^2(x) + \sin^2(x) = 1$$

$$\tan^2(x) + 1 = \sec^2(x)$$

$$\cot^2(x) + 1 = \csc^2(x)$$

SUM IDENTITIES

$$\sin(x + y) = \sin(x) \cos(y) + \cos(x) \sin(y)$$

$$\cos(x + y) = \cos(x) \cos(y) - \sin(x) \sin(y)$$

$$\tan(x + y) = \frac{\tan(x) + \tan(y)}{1 - \tan(x) \tan(y)}$$

DIFFERENCE IDENTITIES

$$\sin(x - y) = \sin(x) \cos(y) - \cos(x) \sin(y)$$

$$\cos(x - y) = \cos(x) \cos(y) + \sin(x) \sin(y)$$

$$\tan(x - y) = \frac{\tan(x) - \tan(y)}{1 + \tan(x) \tan(y)}$$

LAW OF SINES

$$\frac{\sin(A)}{a} = \frac{\sin(B)}{b} = \frac{\sin(C)}{c}$$

DOUBLE-ANGLE IDENTITIES

$$\sin(2x) = 2 \sin(x) \cos(x)$$

$$\cos(2x) = \cos^2(x) - \sin^2(x)$$

$$= 2 \cos^2(x) - 1$$

$$= 1 - 2 \sin^2(x)$$

$$\tan(2x) = \frac{2 \tan(x)}{1 - \tan^2(x)}$$

HALF-ANGLE IDENTITIES

$$\sin\left(\frac{x}{2}\right) = \pm \sqrt{\frac{1 - \cos(x)}{2}}$$

$$\cos\left(\frac{x}{2}\right) = \pm \sqrt{\frac{1 + \cos(x)}{2}}$$

$$\tan\left(\frac{x}{2}\right) = \pm \sqrt{\frac{1 - \cos(x)}{1 + \cos(x)}}$$

PRODUCT TO SUM IDENTITIES

$$\sin(x) \sin(y) = \frac{1}{2} [\cos(x - y) - \cos(x + y)]$$

$$\cos(x) \cos(y) = \frac{1}{2} [\cos(x + y) + \cos(x - y)]$$

$$\sin(x) \cos(y) = \frac{1}{2} [\sin(x + y) + \sin(x - y)]$$

$$\cos(x) \sin(y) = \frac{1}{2} [\sin(x + y) - \sin(x - y)]$$

SUM TO PRODUCT IDENTITIES

$$\sin(x) + \sin(y) = 2 \sin\left(\frac{x + y}{2}\right) \cos\left(\frac{x - y}{2}\right)$$

$$\sin(x) - \sin(y) = 2 \cos\left(\frac{x + y}{2}\right) \sin\left(\frac{x - y}{2}\right)$$

$$\cos(x) + \cos(y) = 2 \cos\left(\frac{x + y}{2}\right) \cos\left(\frac{x - y}{2}\right)$$

$$\cos(x) - \cos(y) = -2 \sin\left(\frac{x + y}{2}\right) \sin\left(\frac{x - y}{2}\right)$$

LAW OF COSINES

$$a^2 = b^2 + c^2 - 2bc \cos(A)$$

$$b^2 = a^2 + c^2 - 2ac \cos(B)$$

$$c^2 = a^2 + b^2 - 2ab \cos(C)$$





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DEFINITIONS

$$\sin(x) = \frac{\text{Opposite}}{\text{Hypotenuse}} \quad \csc(x) = \frac{\text{Hypotenuse}}{\text{Opposite}}$$

$$\cos(x) = \frac{\text{Adjacent}}{\text{Hypotenuse}} \quad \sec(x) = \frac{\text{Hypotenuse}}{\text{Adjacent}}$$

$$\tan(x) = \frac{\text{Opposite}}{\text{Adjacent}} \quad \cot(x) = \frac{\text{Adjacent}}{\text{Opposite}}$$

