

Math 125 Chapter 10/Sections: 10-1 Topic: Systems of Linear Equations

**Definition:** A linear equation is often in the form of  $Ax + By = Cz$ . When there are one or more linear equations, it is known as a \_\_\_\_\_ of linear equations

**Problems I:**

As the CEO of a well-known automotive manufacturer, you and your team celebrated for manufacturing a total of 7 million cars of your top two selling models. The day after, you want to know how many of each model were sold for. From your assistant, they reported that model A and model B sold for a total of \$150 billion. Given that the costs of Model X and Y are \$18,000 and \$24,000 respectively.

Based on the description above, complete the following system of linear equations:

$$x + y = \underline{\hspace{2cm}}$$

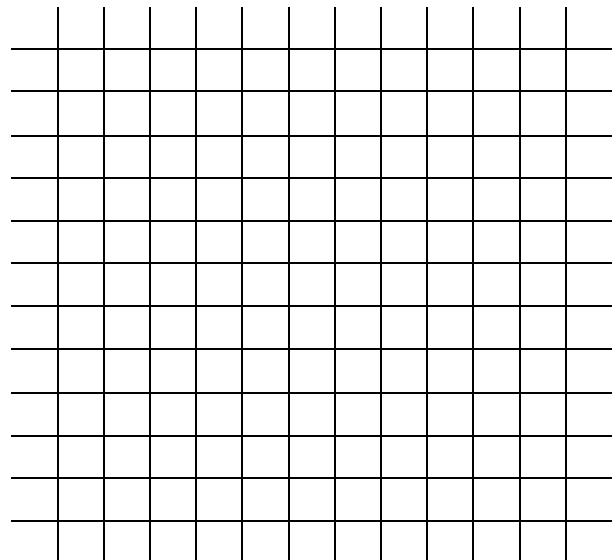
$$\underline{\hspace{2cm}}x + \underline{\hspace{2cm}}y = \$150,000,000,000$$

From the systems of linear equations formed, find the  $x$  and  $y$  intercepts for each line:

$x + y = \underline{\hspace{2cm}}$	
$x$	$y$
0	<u>                    </u>
7,000,000	<u>                    </u>

$\underline{\hspace{2cm}}x + \underline{\hspace{2cm}}y = 150,000,000,000$	
$x$	$y$
<u>                    </u>	$\frac{150,000,000,000}{24,000}$
<u>                    </u>	0

Plot the above points, graph the system of linear equations, find the intersection point, check the estimate.



**Problem II:** From the system of linear equations formed in Problem I, use substitution to solve for  $x$  and  $y$ .

**Problem III:** From the system of linear equations formed in Problem I, use elimination by addition to solve for  $x$  and  $y$ .

**Problem IV:** Solve the following system using elimination by addition. Keep your answers in fraction form. When you are done, make sure the  $x$ ,  $y$ , and  $z$  values satisfy the 3 equations.

$$12x + 2y + 3z = 97 \quad \mathbf{E1}$$

$$-6x + 2y + 8z = 4 \quad \mathbf{E2}$$

$$5x - 2y - 2z = 1 \quad \mathbf{E3}$$

Math 125 Chapter 10/Sections: 10-1 Topic: Systems of Linear Equations SOLUTIONS

**Definition:** A linear equation is often in the form of  $Ax + By = Cz$ . When there are one or more linear equations, it is known as a **system** of linear equations

**Problems I:**

As the CEO of a well-known automotive manufacturer, you and your team celebrated for manufacturing a total of 7 million cars of your top two selling models. The day after, you want to know how many of each model were sold for. From your assistant, they reported that model A and model B sold for a total of \$150 billion. Given that the costs of Model X and Y are \$18,000 and \$24,000 respectively.

Based on the description above, complete the following system of linear equations:

$$x + y = 7,000,000$$

$$18,000x + 24,000y = 150,000,000,000$$

From the systems of linear equations formed, find the x and y intercepts for each line:

$x + y = 7,000,000$	
x	y
0	7,000,000
7,000,000	0

$18,000x + 24,000y = 150,000,000,000$	
x	y
0	$\frac{150,000,000,000}{24,000} = 6,250,000$
$\frac{150,000,000,000}{18,000} = 8,333,333$	0

Plot the above points, graph the system of linear equations, find the intersection point, check the estimate.

$$x = 3,000,000$$

$$y = 4,000,000$$

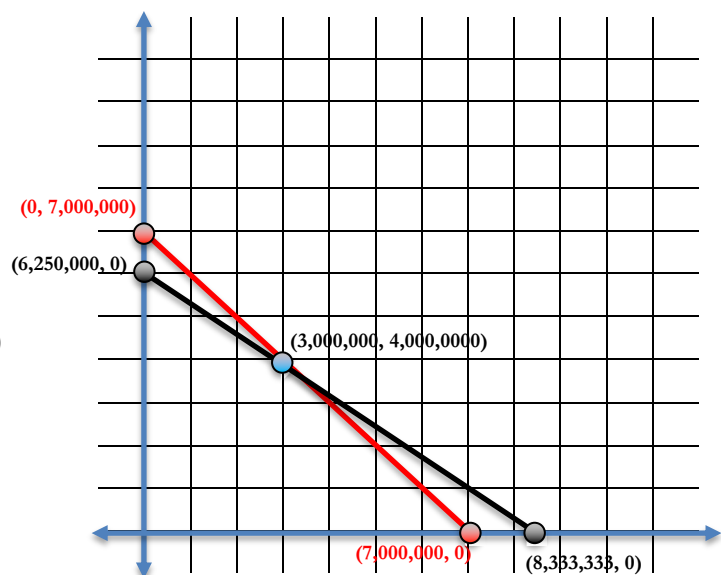
Check:

$$x + y = 7,000,000$$

$$3,000,000 + 4,000,000 = 7,000,000$$

$$18,000x + 24,000y = 150,000,000,000$$

$$18,000(3,000,000) + 24,000(4,000,000) = 150,000,000,000$$



**Problem II:** From the system of linear equations formed in Problem I, use substitution to solve for  $x$  and  $y$ .

1.  $x + y = 7,000,000$
2.  $y = 7,000,000 - x$  # Solve for  $y$
3.  $18,000x + 24,000(7,000,000 - x) = 150,000,000,000$  # Substitute  $y$  into the second equation
4.  $18,000x + 168,000,000,000 - 24,000x = 150,000,000,000$  # Solve
5.  $-6,000x = 150,000,000,000 - 168,000,000,000$  #Solve
6.  $x = -\frac{18,000,000,000}{-6,000} = 3,000,000$
7.  $3,000,000 + y = 7,000,000$
8.  $y = 7,000,000 - 3,000,000 = 4,000,000$
9.  $x = 3,000,000$  and  $y = 4,000,000$

**Problem III:** From the system of linear equations formed in Problem I, use elimination by addition to solve for  $x$  and  $y$ .

#Multiply by a common factor that will cancel one of the variables in the second linear equation

$$\begin{aligned} x + y &= 7,000,000 \\ (x + y = 7,000,000) * -18,000 \\ \hline (-18,000x - 18,000y &= -126,000,000,000) \\ +18,000x + 24,000y &= 150,000,000,000 \\ \hline 0 + 6,000y &= 24,000,000,000 \\ y &= \frac{24,000,000,000}{6,000} = 4,000,000 \end{aligned}$$

$$\begin{aligned} x + 4,000,000 &= 7,000,000 \text{ # Solve for } x \\ x &= 3,000,000 \end{aligned}$$

**Problem IV:** Solve the following system using elimination by addition. Keep your answers in fraction form. When you are done, make sure the  $x$ ,  $y$ , and  $z$  values satisfy the 3 equations.

	$12x + 2y + 3z = 97$ E1	
# Multiply by a common factor that will cancel one of the variables in the second equation. We cancel $x$ .	$-6x + 2y + 8z = 4$ E2	# Find value of $y$
	$5x - 2y - 2z = 1$ E3	$6y + 19\left(\frac{732}{412}\right) = 105$ E4
$12x + 2y + 3z = 97$ E1		$y = \left(\frac{7338}{103}\right)/6$
$-12x + 4y + 16z = 8$ 2 * E2		$y = \frac{7338}{103} = \frac{1223}{103}$
$6y + 19z = 105$ E4		
# Multiply by a common factor that will cancel variable $x$ .		# Find value of $x$
$60x + 10y + 15z = 485$ 5 * E1		$5x - 2\left(\frac{1223}{103}\right) - 2\left(\frac{732}{412}\right) = 1$ E3
$-60x + 24y + 24z = -12$ -12 * E3		$5x = 1 + \frac{2812}{103}$
$34y + 39z = 473$ E5		$x = \frac{2915}{103} = \frac{583}{103}$
# Find value of $y$ or $z$ . We find $z$ .		
# Multiply by common factor		
$204y + 646z = 3570$ 34 * E4		
$-204y - 234z = -2838$ -6 * E5		
$412z = 732$		
$z = \frac{732}{412}$		